NEUTRONIC ANALYSIS OF THE THREE MILE ISLAND
UNIT 2 EX-CORE DETECTOR RESPONSE

by

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Abstract

A neutronic analysis has been made with respect to the ex-core neutron detector response during the TMI-2 incident. A series of transport theory calculations quantified the impact upon the detector count rate of various core and downcomer conditions. In particular, various combinations of coolant void content and spatial distributions were investigated to yield the resulting transmission of the photoneutron source to the detector. The impact of a hypothetical distributed source within the downcomer region was also examined in order to simulate the potential effect of the release of neutron producing fission products into the coolant. These results are then offered as potential explanations for the anomalous behavior of the detector during the period of ~20 minutes through ~3 hours following the reactor scram.
I. INTRODUCTION

The Three Mile Island Unit 2 (TMI-2) reactor experienced an accident on March 28, 1979 which can most easily be described as a small break LOCA (loss of coolant accident). To summarize the now familiar accident sequence in a brief manner, the inadvertent loss of steam generator feedwater initiated a turbine trip and subsequent reactor scram. The continued addition of energy (via decay heat) into a system which had essentially lost its heat sink, led to primary coolant overpressurization. A relief valve opened, properly, in order to vent the excess steam and depressurize the primary loop. This valve failed in the open position—thus the small break LOCA. Further events in the short term, in particular operator actions, did not significantly alter the fact that the system would continue to depressurize and lose great amounts of the coolant inventory through the failed valve. The result was core recovery for a short period of time, along with time dependent voiding and varying water level conditions, specifically within the core and downcomer. A more detailed accounting of the accident progression can be found in Refs. 1-3.

During this time period the ex-core source range neutron detector was exhibiting anomalous count rate behavior. Conjecture following the accident was that one possible explanation for the detector's response would be the changing coolant conditions in the downcomer and core regions. With this hypothesis in mind, a series of neutronic calculations was performed in order to quantify the effects of various potential coolant configurations. The interplay of the downcomer water conditions (which acts primarily as a shield to the detector) and the core coolant state (which determines the photoneutron source and the neutron multiplication factor) will identify those configurations which can lead to significant abnormalities in the detector response.

This report summarizes the work concerning this subject which occurred during a brief period in late summer of 1979. At that point in time, a very small data base existed from which useful conclusions could be drawn. Due to the nature of the accident and the obvious public concern, timely results were of the essence. As such, total consistency amongst all of the items addressed in the results section of this report was not practical. For example, midway through the analysis a modeling improvement was made. Rather than recreating a consistent set of results which incorporated this improvement, its effect was quantified, acknowledged and the progression of calculations continued with the base model now being the improved version. Time constraints precluded any other approach. The impact, however, is not detrimental either to the determination of global trends or the isolation of those conditions which would produce the most significant detector effects.

A. Calculational Methodology

The TMI-2 reactor was modeled in the radial direction out to, and including a portion of, the concrete biological shield. The source range detector is located upon the inner surface of this biological shield at the axial midpoint of the active core. Inasmuch as axial effects are of secondary importance, the model included only a homogenized region of upper and lower internals to act as buffering zones above and below the active core. A vacuum boundary condition was applied to these external boundaries: its
effect upon a more exact solution of the detector response is negligible. Due to the presence of a large air space between the reactor vessel and the detector, it was necessary to utilize a transport theory solution, specifically via the DIF3D\(^4\) code. In view of the fact that large portions of the ex-core structures are modeled, this RZ mockup has much larger memory and running time requirements than for the more typical core only calculations. In particular, a 100 x 90 mesh interval grid was necessary in order to mitigate substantial ray effects and, more importantly, mesh spacing induced instabilities. Thus with running time constraints in mind, the transport theory solution utilized only an S\(_4\)P\(_0\) approximation. Additionally, the energy range group structure was limited to two groups.

The use of a two-group cross section set was not significantly detrimental to the purposes at this work. Some degree of accuracy is lost of course; however, in an LWR environment, it is relatively minor. Moreover, the source range detector is a BF\(_3\) proportional counter - its response depends upon the thermal neutron induced \(\text{H}^{10}(n,\alpha)\text{Li}^7\) reaction which occurs ten times more often than all other reactions combined. The impact of errors in the fast and resonance range of the neutron flux solution is therefore minimized.

The two-group cross section set (thermal cutoff at 1.855 eV) was created via pin-cell calculations with EPRI-CELL.\(^5\) Isotopic cross sections were generated for each of 5 distinct void fraction levels (i.e. 0.0, 0.2, 0.4, 0.7 and 1.0) in order to facilitate more accurate calculations of the partially voided portions of the core. During the first ~2.8 hours of the accident, there was only a small potential for significant core material movement. Therefore, a nominal intact geometry pin cell calculation is generally accurate during the initial phase of the accident, especially until about 2.8 hours after the reactor scram. After this time, the core is hypothesized to be partially intact and partially damaged in some unspecified geometry; however, a regeneration of cross sections to model this departure from nominal geometry was not attempted in this study.

The neutronics model within DIF3D is one of homogenized regions: each distinct core region of interest is a homogenization of fuel, clad and coolant. The calculation, however, retains a pin cell quality due to the spatial and energy self-shielding characteristics which are inherent to the microscopic cross sections via the EPRI-CELL generation. As a result, the homogenized DIF3D run is an adequate approximation to an explicit whole core pin cell calculation. This procedure was benchmarked against both the TMI-2 FSAR and ANL PDQ\(^7\) runs and shown to be quite accurate in reproducing global effects - those effects which will determine the detector response to abnormalities within the core and downcomer.

B. Source Definition

Following the successful scram of the TMI-2 core, there remains several low magnitude neutron sources which will be multiplied, diffuse, and eventually create responses within the source range detector. These sources are identified and quantified for inclusion within the transport calculations.

Spontaneous fission occurs in, primarily, the built up inventory of \(^{249}\text{Pu}\) and \(^{244}\text{Cm}\). The inventory is quite small, however, due to the fact that the incident occurred at approximately only 60 effective full power days of
operation after the initial loading. This source, as calculated via the ORIGEN code\(^{b}\) (point depletion, buildup and decay), amounts to only \(5.4 \times 10^6\) n/sec-core.

A second neutron source results from the interaction of alpha particles with oxygen: \(^{18}\)O + \(\alpha\) + \(^{21}\)Ne + n. Several isotopes undergo \(\alpha\)-decay: \(\geq 98\%\) of the \(\gamma\) emissions in TMI-2 occur in \(^{238}\)Pu, \(^{239}\)Pu and \(^{240}\)Pu. The resulting total neutron source from \(\alpha\)-n reactions is \(-1.22 \times 10^7\) n/sec-core.

There are two discrete startup sources in the TMI-2 core: they are reported to be standard Am-Cm-Be type with an initial strength of \(1.4 \times 10^7\) n/sec apiece. At the time of the accident, the strengths are down to \(-10^5\) n/sec each (see Ref. 7), yielding a total of \(-2 \times 10^5\) n/sec-core.

A major source during the short term is the decay of the full power flux level and delayed neutrons. At shutdown, the average total flux level is \(-2.8 \times 10^{14}\) n/cm\(^2\)-sec. Using a 6-group point kinetics approximation and a very conservative value for the shutdown \(k_{\text{eff}}\) (0.98 as opposed to the nominal value of 0.92), the full power flux level and delayed neutron level falls to about \(1000\) n/cm\(^2\)-sec in 30 minutes. [For comparison, an external source of \(2 \times 10^5\) n/sec will produce a flux level on the order of \(-10^3\) n/cm\(^2\)-sec (Ref. 8)]. Several minutes later, this value is totally negligible. This source, therefore, is of little consequence during the time frame of interest.

The last neutron source of any consequence is that from photoneutrons. Gamma interaction with the trace amount of deuterium in the coolant \((D/H = 0.00015)\) leads to a \(D(\gamma,n)H\) reaction. Due to the massive amount of \(H_2O\) present, this trace reaction produces a sizable neutron source. One estimate based upon order of magnitude assumptions for 1 hour after SCRAM is \(10^{10}\) n/sec (Ref. 7). A more accurate estimate was made by combining the explicit \(\gamma\) emission spectrum and rate from an ORIGEN calculation with the physical constants of the system: D fraction in \(H_2O\), fraction of released \(\gamma\)'s which are absorbed in \(H_2O\) (12.6\%, see Ref. 9), the \((\gamma,n)\) cross section for D, etc. The result is the time dependent photoneutron emission curve depicted in Fig. 1. In this case, the estimate at 1 hour after scram is \(\sim 10^{11}\) n/sec. As can be seen, there is a considerable time variation during the period of interest: from 1/2 hour to 3 hours the photoneutron emission rate decreases by a factor of 4.5.

To summarize the neutron source definition, it appears that all sources are negligible with respect to the photoneutron and start-up sources. Between these two, the photoneutron source dominates for about the first 12 hours after the scram. Subsequent decay of the \(\gamma\) emitters then leads to the start-up source providing a "base level" below which the neutron source will not fall. A numerical summary is provided below in Table I.

It should be emphasized at this point that the precise value of the photoneutron source is of secondary importance when compared to establishing the time variation and the order of magnitude estimate for the source. In the first place, it was necessary to identify the dominate neutron source within the system: Table I clearly displays that the photoneutron source is the controlling neutron source during the short term. Secondly, the time variation of this source indicates that it will dominate for several hours.
Therefore, the analysis concerning the first few hours after the scram can be based upon this source alone. Further, the exact count rate of the detector is never inferred from this analysis, rather the relative change in the number of detector absorptions is utilized. Thus, the impact of the exact magnitude of photoneutron source is minimized. As a consequence, a more precise estimate of the source is not required.

C. Calculational Model

The simplified geometrical and material layout of the TMI-2 calculational model is described in this section. It is essentially identical to
the standardized model utilized by the Nuclear Safety Analysis Center (operated by the Electric Power Research Institute) during 1979. An RZ map and dimensions are provided in this section. The more detailed number density and volume fraction information is presented in Appendix A. In order to put the following into perspective, a scale drawing of the near core structures is provided in Fig. 2.

![Fig. 2](image)

As mentioned previously, the core zones are a homogenization of fuel, clad and coolant. More globally, this homogenization extends throughout the core to include each of the 3 distinct batches of fuel: the result is a core material with an average initial enrichment of 2.57 wt.% $^{235}\text{U}$. In anticipation of the introduction of a spatial void distribution, the core is divided axially into 5 zones. The 12 foot high core has a 1 foot layer of upper internals above and a similar 1 foot layer of lower internals below. In both cases, the internals are represented by an appropriate mixture of coolant and steel.

Adjacent to the core is a downcomer region which extends the entire axial length of the model. This region is a homogenization of the core barrel, water gaps, thermal shield, core liner and the downcomer region proper. It, like the core, is divided into axial zones in order to facilitate spatial studies. This region is ~74% water and ~26% stainless steel, its width is approximately 53 cm (~1 ft.). The reactor vessel is next, consisting of carbon steel and being ~21 cm thick (8-3/8 in.). These two regions alone account for the bulk of the shielding of the source range detector from core neutrons.

The biological concrete shield surrounds the reactor vessel at a distance of 112 cm (3.8 feet). Its nominal thickness is 4.5 feet, however, only several mean-free paths of material is modeled in order to provide a sufficient boundary condition. Upon this shield is the source range detector.
Figure 3 illustrates the full RZ calculational layout with appropriate dimensions; also, a detailed expansion of the detector area is depicted in Fig. 4.

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The photoneutron source was approximated by applying a uniformly distributed volumetric neutron source throughout the core. The nominal volumetric source strength was chosen to be $6.25 \times 10^3$ n/cm$^3$-sec. With a core volume of
$3.0826 \times 10^7 \text{ cm}^3$, the inferred total photoneutron source is $\sim 1.9 \times 10^{11} \text{n/sec-core}$. This value corresponds to our estimate of the photoneutron strength at about 30 minutes after the scram (see Fig. 1). It is thus an adequate initial value. The time variation of this can be easily factored in when applying the results in part II to times other than this. Additionally, the neglect of the spatial distribution of the photoneutron source should be a second-order effect due to the large mean-free paths of the high energy photons ($>2.2 \text{ MeV}$) necessary to initiate the threshold $\text{D(\gamma,n)H}$ reaction. The reduction of the source strength due to core voiding is approximated by reducing the nominal value by the factor $(1-\nu)$, with $\nu$ representing the void fraction.

It is also noted that the RZ calculational model necessarily yields an annular detector region rather than the actual discrete cylindrical shape. Thus, the results section will quote detector absorptions which are too large by a factor equal to the ratio of the volumes of the calculational model detector and the actual detector. This ratio is approximately 201.6.

II. RESULTS

The results of various static calculations are provided in this part. When significant model changes are introduced, they will be highlighted. If not mentioned, they will have failed to have an appreciable impact upon the detector response.

A. Homogeneous Voiding Effects

One of the more straightforward effects of the accident is the initial phase when the system was depressurizing during continued heat input via decay heat. There existed a sizable potential for the formation of relatively homogeneous voids within the primary loop. Upon to the point of pump cavitation, or de-energization, the fluid would be relatively uniform in nature both in the core and downcomer. In order to quantify the interplay of the core voiding and the downcomer voiding effects, a sequence of homogeneous void calculations was created.

The reactor system was benchmarked at $k_{\text{eff}}$ equal to unity with the rods out and $\sim1700$ ppm of soluble boron present. (This level of soluble boron also accounts for the burnable poisons, $\sim 1.4\% \Delta k/k$.) With the control rods inserted, again their worth was represented by boron, $k_{\text{eff}} = 0.92$. From this assumed shut-down position (with a total boron level of 2600 ppm), calculations were made containing void fractions of 0.2, 0.4, 0.7, 0.9 and 1.0, respectively. The void fractions were applied uniformly to the core, downcomer, upper and lower internal regions. The system eigenvalues are listed in Table II and are also illustrated in Fig. 5. Results for the cases near 100% void may be subject to error due to the extreme nature of the problem, however, the value of 0.313 for a dry core is consistent with typical values.

As the core voids, the photoneutron source decreases in strength concurrently with an increase of the leakage probability. More importantly, however, is the loss of "shielding" which occurs as the downcomer region voids. Even though the neutron source strength is decreasing, the transmission probability (i.e. to the detector) is increasing at a greater rate. The
TABLE II. Homogeneous Void Results

<table>
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<tr>
<th>Void Fraction</th>
<th>k\textsubscript{eff}</th>
<th>Source Neutron Absorption Probability in Detector\textsuperscript{a}</th>
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</thead>
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<tr>
<td>0</td>
<td>0.920</td>
<td>$1.57 \times 10^{-7}$</td>
</tr>
<tr>
<td>0.2</td>
<td>0.917</td>
<td>$6.34 \times 10^{-7}$</td>
</tr>
<tr>
<td>0.4</td>
<td>0.896</td>
<td>$2.85 \times 10^{-6}$</td>
</tr>
<tr>
<td>0.7</td>
<td>0.780</td>
<td>$3.67 \times 10^{-5}$</td>
</tr>
<tr>
<td>0.9</td>
<td>0.650</td>
<td>$2.46 \times 10^{-4}$</td>
</tr>
<tr>
<td>1.0</td>
<td>0.313</td>
<td>$1.88 \times 10^{-3}$</td>
</tr>
</tbody>
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\textsuperscript{a}Detector Model — which is actually a ring around the vessel due to the P2 geometry, the ratio of actual detector volume to the model's volume is $4.961 \times 10^{-3}$.

Fig. 5. Eigenvalue vs. Homogeneous Void Fraction
result is a continually increasing count rate. Figure 6 illustrates the results for the detector absorptions (which, of course, are proportional to the count rate) vs. void fraction. The calculation of a value for a void fraction near 1.0 is not presented inasmuch as it would be highly speculative. (That is, the exact value of the total source strength is some combination of very low order source strengths once the predominate photon neutron source is essentially eliminated, and is therefore difficult to quantify accurately.) As can be seen, homogeneous voiding can account for a maximum increase in the count rate of a factor of about 40. The transmission probability is defined as the ratio of the detector absorptions and the total neutron source. This quantity is shown in Fig. 7.

![Graph](image1)

Fig. 6
Detector Absorptions vs.
Homogeneous Void Fraction

![Graph](image2)

Fig. 7
Transmission Probability vs.
Homogeneous Void Fraction

B. Inhomogeneous Voiding Profiles

The usefulness of the homogeneous voiding data is restricted to the first ~1-1/2 hours following the scram. Following this time, various initiating events, primarily the de-energization of the A loop pumps, caused several diverse thermal hydraulic effects to occur: among them were temporary flow stagnation, vapor/fluid separation, spatially dependent voiding within the core, etc. This area of analysis is by nature much more speculative than in part A. However, reasonable assumptions can lead to data from which general trends and global effects can be quantified. The following
subsections describe three separate voiding model assumptions which were utilized in order to accomplish this.

1. **Model 1 - 40% Maximum Void Up to Boil-off Interface, 100% Void Above**

Based upon various thermal hydraulic considerations and the physical constants (specifically pressure and temperature) which were present during the 1-1/2 to 3 hour period following the scram, it has been suggested that the core could have created a "stable" void profile in the axial direction. That is, there would be enough heat generated to create and maintain a certain maximum void fraction level. In particular, one hypothesis is that the void fraction would increase from 0.0 at the bottom of the active core to ~0.4 in about 2 to 3 feet. (Model 1 utilized a linear relation terminating arbitrarily at 2.44 feet.) Above this height, the void fraction would remain constant at this maximum value until the boil-off interface is encountered. Above this interface, the void fraction is assumed to be 1.

An additional and extremely important feature of this model is that the downcomer void fraction falls to zero after pump shutdown. The water level in the downcomer is then dependent upon the gravity head in the core. Due to the presence of the voids within the core, the downcomer water level is always lower than the coolant level in the voided core/upper internals region during this period (i.e. of low coolant inventory and absence of forced circulation).

The relative heights of the downcomer and core regions were adjusted in the calculational model (consistent with the above gravity head constraint) so that discrete points during a hypothesized boil-off process could be calculated. The resulting count rates are once again, as during the homogeneous voiding process, a product of the interplay of the changing source strength in the core and both the amount and the location of the shielding provided by the downcomer water. This is best illustrated by examining the detector absorption vs. downcomer water level curve in Fig. 8.

As the downcomer water level approaches the top of the active core (12 feet), the count rate increases only slightly due to the increased transmission probability for the source which scatters and diffuses out of the top of the core. The next point of interest is when the downcomer level has lowered to a point of ~7.7 feet; at this point the gravity head of the nonvoided downcomer region exactly matches that of the voided core. The detector absorptions increase very rapidly over this range as the core source strength remains essentially constant while the downcomer shielding is removed. When the downcomer level lowers further, the core water level now decreases or boils off as it continuously matches the gravity head of the downcomer. The detector absorption curve continues to rise, however, due to the fact that the core source strength is decreasing in a low worth area (i.e. the upper two feet of the active core) while the downcomer shielding is being removed at the point of its highest worth - near the 6 feet level. (The detector is located at the axial midpoint of the core - 6 feet height.) Subsequent decreases in the water level begin to substantially decrease the source strength with respect to the benefit of reduced shielding; the detector absorption rate thus begins to decrease. The maximum/minimum count rate ratio for the model 1 curve is ~320.
In an effort to verify that, for example, subtle mesh instabilities or ray effects were not disturbing the \( S_{\text{NP}} \) calculation, four sample calculations were repeated utilizing the VIM\textsuperscript{10} Monte Carlo code. VIM has been successfully utilized in benchmarking an LWR lattice,\textsuperscript{11} and more importantly, accurately removes those calculational problems which are inherent in a transport solution. Especially with respect to the large air gap between the vessel and the detector, the Monte Carlo solution is clearly superior. In order to isolate strictly calculational problems, the transport result was normalized to the VIM boron cross section values in order to produce corresponding detector absorption rates. The results are listed in Table III.

It can be seen that no appreciable problems are evident in the transport calculation. Indeed, considering the severity of the problem from a quadrature point of view, the comparison is excellent. It appears from Table III that the transport model is of sufficient detail to expose the proper detector response trends to various core/downcomer conditions.
<table>
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<th>Case</th>
<th>Core Water Level (feet)</th>
<th>Downcomer Water Level (feet)</th>
<th>( S_N (\times 10^{-5}) ) Detector Abs./Total Source</th>
<th>( \text{VIM} (\times 10^{-5}) )a Detector Abs./Total Source</th>
<th>( \text{VIM-S}_0 ) Std. Dev.</th>
<th>( \text{VIM} ) Eigenvalue( b )</th>
<th>Number of Histories (Thousands)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>12.0</td>
<td>7.0</td>
<td>4.48</td>
<td>3.98 ( \pm ) 6.4%</td>
<td>2.0</td>
<td>0.9136 ( \pm ) 0.0023</td>
<td>80</td>
</tr>
<tr>
<td>2</td>
<td>9.9</td>
<td>6.4</td>
<td>7.50</td>
<td>5.84 ( \pm ) 6.9%</td>
<td>4.1</td>
<td>0.9115 ( \pm ) 0.0025</td>
<td>50</td>
</tr>
<tr>
<td>3</td>
<td>4.7</td>
<td>3.3</td>
<td>8.76</td>
<td>8.65 ( \pm ) 5.9%</td>
<td>0.2</td>
<td>0.8966 ( \pm ) 0.0030</td>
<td>55</td>
</tr>
<tr>
<td>4</td>
<td>2.4</td>
<td>2.0</td>
<td>7.50</td>
<td>7.87 ( \pm ) 4.6%</td>
<td>-1.0</td>
<td>0.8475 ( \pm ) 0.0018</td>
<td>100</td>
</tr>
</tbody>
</table>

a Track length estimator

b Analog plus track length estimator
2. Model 2 - 30% Maximum Void Up to 
Boil-off Interface, 95% Void Above

The particular assumptions in Model 1 are based upon sound engineering judgment, but are none the less arbitrary. In order to quantify the sensitivity of the detector response to variations in the major assumptions, this second (and subsequently a third) model is introduced. The maximum allowed void level is reduced to 30%: again the void fraction increases linearly from 0 at the bottom of the active core to 0.3 at a height of 3 feet. The height of the boil-off interface again depends upon the gravity head of the downcomer, however, the voided region above and/or within the core is assumed to contain steam and water droplets, thus the 95% maximum void value above the boil-off interface. The calculational model's zone boundaries were adjusted from those in Fig. 3 so that the gravity head constraint was satisfied at various downcomer/wet core region combinations. The photoneutron source is again proportional to \((1-v)\), with \(v\) representing the void fraction, and is spatially uniform in distribution.

A progression of calculations was made in a similar manner to Section II.B.1 in which the water level was sequentially lowered in the downcomer region - the core level followed at the appropriate level. The results are depicted in Fig. 9, which also contains the Model 1 results for comparison. The two curves are very similar until the point of core uncoverly is reached: apparently, to the first order, the increased source strength in Model 2 is roughly balanced by increased self-absorption in the water. Due to the lower void fraction, the downcomer gravity head cannot support as large a height of core as its corresponding point in model 1, thus core uncoverly occurs at a higher downcomer level. Given identical downcomer heights, Model 2 exposes smaller axial portions of the wet core region, thus relatively lower detector absorptions despite higher volumetric photoneutron sources. For example, when the downcomer is at the 6 feet level, Model 2 predicts that two feet of wet core will be exposed to the detector while Model 1 predicts ~3.3 feet. Although Model 2 has a volumetric source strength which is 16.7% greater than Model 1, the exposed area is 40% less; hence lower count rates. When the water levels are decreased further, the second difference in the models becomes apparent. At very low water levels, the wet core source is of low worth and the dried

*For purposes of this discussion, the portion of the core which contains significant amounts of water (i.e. \(v < 0.4\)) will be referred to as wet.
out bulk of the core dominates the detector response. Model 1, although at 100% void, contained a volumetric neutron source 1/100 of the nominal photo-neutron source in order to model the start-up source. Model 2, of course, has an assumed void fraction of 0.95 in the dried out area: the source strength is therefore 5% of nominal, or a factor of five higher than Model 1. As a result, the detector absorptions are higher for Model 2 at very low water levels.

The differences between the two models, however, are relatively small on a global basis. The detector response is not particularly sensitive to nominal sized changes in the specific assumptions. For Model 2, the max/min count rate ratio is ~225. This compares with a value of 320 with Model 1—a decrease of 30% with respect to Model 1. The difference, however, is smaller and less important than it seems at first. A significant portion of the shift (11% of the 30%) is due solely to the small difference in the respective minimum values. This has little consequence upon any conclusions concerning the core uncovery process. More importantly, though, is the fact that global trends are the desired result. It would be inappropriate to claim, for example, that the core voiding and uncovery process can produce a change in the count rate of a factor of specifically 320. It is quite clear, however, that this process can produce increases in excess of two orders of magnitude. This then, is the proper way in which to view the results.

An interesting way to examine the impact of the exposed wet core is shown in Fig. 10. In it, the detector absorptions for the two models are illustrated as a function of the differential between the downcomer water level and the wet core level. The importance of the location of the exposed wet core area is evident as the maximum detector absorptions do not occur at the point of maximum exposed wet core. This figure also demonstrates that the maximum amount of exposed wet core always occurs at the point of the initiation of core uncovery.

![Fig. 10](image-url)

Detector Absorptions vs. Wet Core/Downcomer Water Level Differential
3. Model 3 - 40% Maximum Void Up to Boil-off Interface, 95% Void Above, Axially Distributed Photoneutron Source Utilized

This third model combines what is considered to be the two most likely aspects of the previous models: i.e. a 40% maximum void level in the wet core regions with a 95% maximum void level in the dried out regions. The major difference is provided by the replacement of the spatially uniform distribution of the photoneutron source with a more realistic axially dependent source distribution. The photoneutron source will, to the first approximation, follow the fission product (thus power) distribution. The radial dependence is neglected as its effect will not alter the calculated trends, only the absolute magnitude of the count rate. However, given the results of the first two models which indicate a fairly sensitive interplay of source strengths and water levels, it is possible that an axially dependent source could alter the global trends. It is this concern that predicates this third model.

Model 3 has the void fraction increase linearly from 0 to 0.4 over the lower 4 feet of the active core height. The calculational model zone boundaries in the core and downcomer were again adjusted so that the gravity head constraint was satisfied. Physics calculations provided by TMI-2/Metropolitan Edison personnel for the core as of March 19, 1979 yielded the predicted axial power distribution. This power distribution is then assumed to be equal to the fission product distribution, and thus the photon source. The data is listed below in Table IV.

<table>
<thead>
<tr>
<th>Core Height (feet)</th>
<th>Interval Power Level (kW/ft)</th>
<th>Normalized to 100</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1.71</td>
<td>5.38</td>
</tr>
<tr>
<td>1.71 + 3.43</td>
<td>9.14</td>
<td>14.39</td>
</tr>
<tr>
<td>3.43 + 5.14</td>
<td>10.24</td>
<td>16.13</td>
</tr>
<tr>
<td>5.14 + 6.86</td>
<td>10.74</td>
<td>16.91</td>
</tr>
<tr>
<td>6.86 + 8.57</td>
<td>11.00</td>
<td>17.32</td>
</tr>
<tr>
<td>8.57 + 10.29</td>
<td>10.28</td>
<td>16.19</td>
</tr>
<tr>
<td>10.29 + 12.00</td>
<td>6.72</td>
<td>10.58</td>
</tr>
</tbody>
</table>

An inspection of a sample of various other assembly locations in the core revealed that the centerline distribution was fairly representative. The normalized axial power distribution is illustrated in Fig. 11. This distribution was applied by renormalizing it to the total neutron source which was assumed in Models 1 and 2. Thus, in a nonvoided configuration, the axially distributed source would produce the same total number of photoneutrons within the core as the uniform distribution does. During voiding and subsequent dry out, however, the sources will differ as the void dependent term $1-v$ will be acting upon different local source strengths. The renormalized source strengths for a nonvoided configuration are listed in Table V.
Fig. 11. Axial Power Distribution in TMI-2 Center Assembly
TABLE V. Axially Dependent Photoneutron Source Density for the Calculational Model

<table>
<thead>
<tr>
<th>Calculational Core Region</th>
<th>Height (feet)</th>
<th>Axially Dependent, $\times 10^3$</th>
<th>Uniform, $\times 10^3$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>0</td>
<td>4.60</td>
<td>6.25</td>
</tr>
<tr>
<td>2</td>
<td>1.71</td>
<td>7.00</td>
<td>6.25</td>
</tr>
<tr>
<td>3</td>
<td>3.43</td>
<td>7.44</td>
<td>6.25</td>
</tr>
<tr>
<td>4</td>
<td>5.14</td>
<td>7.44</td>
<td>6.25</td>
</tr>
<tr>
<td>5</td>
<td>6.86</td>
<td>7.22</td>
<td>6.25</td>
</tr>
<tr>
<td>6</td>
<td>8.57</td>
<td>6.32</td>
<td>6.25</td>
</tr>
<tr>
<td>7</td>
<td>10.29</td>
<td>3.63</td>
<td>6.25</td>
</tr>
<tr>
<td>8</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Figure 12 illustrates the results of Model 3. The minor differences from Model 1 are relatively easy to explain. The lower values during the initial lowerering of the downcomer level are due to the importance of the source in the upper region of the core. Due to the axial distribution, it is lower with respect to the uniform distribution. Once the middle portion of the wet core becomes exposed, the advantage shifts to Model 3 as the higher source density regions in the center area lead directly to higher count rates. The higher detector absorptions at very low water levels is a result of the assumption of a maximum void fraction of 0.95 in the dried out portion of the core. This higher photoneutron source with respect to Model 1 makes up for the fact that the Model 3 source in the lower core region is smaller than in the uniform distribution. The count rate max/min for this model is ~300: the conclusions mentioned in Section II.B.2 concerning two orders of magnitude increases in the count rate due to core uncover-ery are still valid.

C. Intermediate Range Detector Response

The intermediate range detector has a considerably different geometry from the source range detector. It has a 4-in. lead shield as opposed to 2-in. and its active height is 14 in. rather than 26 in. The diameter of
the BF$_3$ zone is the same as the source range detector. As a result, the above changes effectively move the centerline of the detector 2.1 in. closer to the reactor vessel. In consideration of the possibility that the differing geometry could yield an altered response, five cases were recalculated utilizing Model 3 assumptions with the source range detector replaced by the intermediate range geometry.

The five resulting data points are shown on Fig. 12. As is expected from the presence of increased shielding from the lead and the decrease in active detector volume, the count rates decrease with respect to the original Model 3 results. Incidentally, the decrease is by almost a uniform amount of ~40%. No surprising trends or variations are evident from this permutation of the detector geometry. In addition to indicating that the intermediate range detector should respond in a similar manner as the source range detector does, the results indicate that the basic global trends are not acutely dependent upon the specifics of the detector model.

### D. Impact of Downcomer Bypass Region and Released Source in Downcomer

Two relatively straightforward permutations are addressed in this section. First, the downcomer region is split into 2 radial zones: the inner zone is allowed to follow the core void fraction and height. The second effect is the impact upon detector response which a distributed source within the downcomer region has.

#### 1. Effect of a Split Downcomer Region

It has been postulated that the bypass region of the reactor would receive sufficient heat that it would follow the core configuration rather than the downcomer. Up to this point, the bypass region has been lumped together with the other regions between the reactor and its vessel. Thus a massive calculational "downcomer" region. In this model, the bypass region (radius of 163.8 + 179.1 cm) is allowed to exhibit the void fraction and wet level of the core. The outer downcomer (radius of 179.1 + 217.2 cm) acts as it did previously.

Results for this calculation are shown in Fig. 13. Basically, the bypass region acts to shield the exposed area of wet core as it follows its level exactly and count rates are decreased over the entire curve with respect to Model 1. The exception is when the downcomer is completely filled and there is no exposed wet core to shield. In this case, the voided bypass region increases transmission slightly and therefore increases count rates. The approximate max/min is reduced to ~75.

#### 2. Effect of A Hypothetical Source Within the Downcomer

There exists the possibility that following core uncover, fission products became distributed within the downcomer water as a result of global fuel pin failure via clad oxidation and embrittlement. Fission products within the downcomer water would cause photoneutron sources which are significantly more effective with respect to detector absorption than those within the core. The magnitude of the source, however, probably would not be that large with respect to the total core source. For example, the combination
of assumed fission product release fractions and subsequent dilution within
the coolant inventory could easily reduce the potential source to <10% of
the theoretical core maximum. With this in mind, the potential effectiveness
of a neutron source within the downcomer was quantified by placing a
uniform distribution of the nominal photoneutron source at arbitrary values
of 1% and 2% of the full strength value.

The effect of this source is seen in Fig. 14 as the above model
of Section II.D.1 was utilized. When the downcomer is relatively full and
substantially shielding the core, the newly placed source has a significant
impact upon the count rate. With the downcomer fully filled, the count rate
is increased by factors of 4 and 7, respectively, with respect to the results
without a downcomer source. As the wet core is exposed, the source from the
core outweighs the source from the downcomer. At the point of core uncover
(downcomer at 8 feet), the count rates among the three cases are within ~20%
of each other. After further uncover, the 3 curves merge. The effect of
the downcomer source is primarily to alter the minimum count rate; thus the
max/min ratio for the 1% and 2% cases are merely ~14 and ~6, respectively.
The maximum value is left unchanged.
Fig. 14. Effect of a Hypothetical Source Within Downcomer - Detector Absorptions vs. Water Level
III. SUMMARY

The results in part II quantify estimates of the detector count rate changes which can be expected from various combinations of water conditions within the core and downcomer regions. They will now be linked to the actual response of the detector in order to provide possible interpretations for the anomalous count rate behavior. Figure 15 illustrates the TMI-2 source range detector's response up to four hours following the scram.

![Graph of detector response](image)

Fig. 15. Ex-Vessel Source Range Detector Response: 0 + 4 hours

A. Period of Approximate Homogeneous Voiding (0 to 1 hour 40 minutes)

The anomalous behavior is initiated at ~30 minutes when the detector count rate ceases a normal monotonic descent and starts to slowly increase. The subsequent period of relatively gradual increases ends abruptly at ~1 hour 40 minutes. During this time period, the primary system is depressurizing and losing coolant through the failed block valve. Excessive pump vibrations lead to the de-energization of the B loop pumps at about ~1 hour and 14 minutes, the A loop pumps at ~1 hour 40 minutes (each loop has 2 pumps). The combination of pressure, heat source, lack of heat sink and low coolant inventory could have led to the initiation of voiding within the core. As time progressed, the voiding could have spread throughout the entire primary loop. The driving force of the pumps would have tended to maintain fairly uniform void profiles within the system, specifically within the core and downcomer. Therefore until the final pumps were de-energized, an approximate uniform void condition could have begun with gradually increasing void content with respect to time.
The maximum change in count rate over this period of time is approximately a factor of 15 increase (6000/400 = 15, see Fig. 15). The results for homogeneous voiding in Section II.A indicate that a maximum increase in the count rate of a factor of ~40 could be experienced if the void fraction increased from 0 * 0.95. However, a void fraction of 0.95 would have been difficult to achieve. Pump cavitation is predicted to occur near ~60% void content. Correspondingly, the excessive pump vibration which resulted in the decision to de-energize the last remaining coolant pumps was indicative of pump cavitation. Therefore, a more realistic prediction of the maximum increase in count rate would be the change depicted in Fig. 7 between a void content of 0 and ~60%: an increase by a factor of ~20 is predicted. Photoneutron decay over this time period would reduce this value to ~11 (see Fig. 1). This value demonstrates the credibility of the homogeneous voiding scenario over this time period as it compares favorably with the actual increase of a factor of 15.

8. Period of Inhomogeneous Voiding and Coolant Level Irregularities (>1 hour 40 minutes)

Following the de-energization of the last remaining pumps at 1 hour 40 minutes, various events during the next few hours lead to inhomogeneous voiding and rapidly changing water levels. The more obvious initiating events are the restarting of primary loop pumps or actuation of the ECCS - both provide rapid influxes of water to the downcomer and core. More subtle changes also impact the detector response: block valve reclosure, possible core rearrangement, spatially inhomogeneous voiding, etc. All of these events, and potentially some as yet unspecified ones, interacted to yield the actual time dependency of the detector response. The inhomogeneous voiding results from part II.B and D are now utilized to provide possible interpretations of the detector response after 1 hour 40 minutes.

At the time of the last A loop pump de-energization, the count rate had reached a local maximum of ~6000 cps. There follows on Fig. 15 an almost immediate drop to the minimum value of 160 cps - a factor of 37.5 decrease. This can be explained by considering that the homogeneously voided coolant would undergo a phase separation when the pump's driving force is eliminated: solid water would fall to fill the downcomer - thus effectively shielding the detector. [The decay of the photoneutron source is negligible during these few minutes, thus values need not be corrected for time effects.] The effect of instantaneous collapse of a homogeneously voided core/downcomer can be extracted directly from Fig. 6.

However, an instantaneous collapse is impossible to achieve due to the pressure drop within the core: the downcomer would most likely refill prior to 100% refill within the core. Thus, the nonvoided downcomer would be shielding the detector from a core which had less of a photoneutron source than the instantaneous collapse model predicts. The result, of course, is lower count rates for a short time as the core completes its refill process: this results in an increase in the effective count rate reduction factor from that value which would be predicted via the instantaneous model. Viewed in this fashion, it can be seen that reduction value factors extracted from Fig. 6 (say, e.g., 20 + 35) then compare favorably with the detector decrease of ~37.5.
The next portion of the count rate response to be examined is the period from the minimum achieved count rate (160 cps at ~1 hour 42 minutes) to the point at which the B loop B pump was restarted at 2 hours 53 minutes. This period of time first has a marked increase in count rate over a short time period (increases by a factor of 100 over ~20 minutes) and then, after reaching a maximum near the 2 hour 23 minutes mark, decreases less rapidly (by only a factor of ~2.3) until the point at which a B loop pump was restarted. This portion of the curve is compared directly with the results depicted in Figs. 8, 9, 12 and 13; i.e. Models 1, 2 and 3.

The accident, at this point, was still a small break LOCA as the block valve was not reclosed until near the 3 hour mark. With the absence of forced circulation, the decay heat was removed via natural circulation. Unfortunately, there did not exist a sufficient coolant inventory to accommodate this process due to the depressurization and steam venting. As a result, core boil-off most probably ensued. The effect of this particular process was quantified in the above mentioned figures: the results have two salient features. First, that the downcomer level has the most immediate and significant impact upon the detector response. [All of the figures reflect this, however, Fig. 12 will be utilized as a source to provide quantitative examples.] The downcomer level drops as the core undergoes the voiding process. The count rate increases, e.g., by a factor of ~100 as the downcomer drops just 3-1/2 feet below the top of the active core. The total max/min factor is 300. This illustrates that the position of the downcomer can easily account for the actual count rate response increase of a factor of 100. Specifics of exactly where the downcomer water level is with respect to time and count rate is not feasible within the context of this approximate work. However, all results clearly illustrate that a factor of 100 increase in the count rate is achievable during the initial phase of core boil off. Even the inclusion of a split downcomer region (Fig. 13) does not preclude a two order of magnitude increase in the count rate.

The second important feature of the inhomogeneous results is the possibility that the slowly decreasing count rate could be the result of continued core boil off once the maximum count rate value has been reached. The shape of the count rate response during this period of time (~1:50 + 2:50) qualitatively matches that of the results presented in Section II.B. Of course, a gradual refill in the downcomer or the core region could produce the decreasing count rate, too. It would be too speculative to conjecture which scenario is more likely. Nevertheless, the boil off process and the downcomer water level can explain the detector behavior qualitatively over the period of 1 hour 40 minutes to 2 hours 53 minutes, at which time a B loop pump restarted and initiated further developments.

Subsequent events can be interpreted in a similar fashion to the above. The startup of a B loop pump delivered flow to the downcomer for approximately 8 seconds - in an analogous fashion to the phase separation and downcomer refill described earlier, an immediate and substantial decrease in the count rate is expected and seen in Fig. 15. Similarly, the ECCS actuation at ~3 hours 20 minutes leads to a rapid decrease in count rate as the downcomer is again refilled. Following each of these events, count rate variations can be expected due to the possibility of water level readjustment, core rearrangement, fission product release, small scale boil off, etc. A combination of
quantified effects from Section II can be utilized to explain the trends and, to some extent, the magnitudes of the count rate changes in Fig. 15.

As discussed above, most of the anomalous neutron detector readings could be correlated with the known sequence of events, and some inferences could be made with respect to the core hydraulic conditions. However, because the core neutronic and hydraulic conditions during the TMI-2 incident are not precisely known, uncertainties are introduced and explicit quantitative analyses of the detector response do not appear feasible. Nevertheless, the detector response is important information which, along with other instrumentation data and thermal-hydraulic analyses, could be correlated in order to provide a self-consistent scenario of core conditions during the TMI-2 incident.

IV. ACKNOWLEDGMENTS

The authors gratefully acknowledge the assistance provided by C. H. Adams, K. Fujita, E. M. Gelbard and L. J. Milton, who provided considerable calculational and advisory assistance during the relatively short period of time over which this work had to be completed. Also, R. Henry and P. Abramson are recognized for furnishing the spatially dependent void profile model and other thermal-hydraulic information.
V. REFERENCES


APPENDIX A: CALCULATIONAL MODEL MATERIAL DESCRIPTION

The calculational model which was utilized in this work is described in a general fashion in Section I.C. This appendix presents the more detailed specifics of the materials which comprise the model.

As mentioned previously, the model which was utilized by the Nuclear Safety Analysis Center (NSAC, operated by the Electric Power Research Institute) was adopted in order to provide some degree of consistency with other calculations. Table A-1 reflects this information as it lists the materials and volume fractions appropriate for each region. The region numbers correspond to those in Fig. 3, which is included here as Fig. A-1. The detector region (number 17) is shown in expanded detail in Fig. A-2: the three detector materials (lead shielding, polyethylene and BF$_3$) each have a volume fraction of 1.0 within their respective subregions.

<table>
<thead>
<tr>
<th>Region Number</th>
<th>Region Description</th>
<th>Basic Materials Present</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Upper Core Internals (includes outlet plenum, etc.)</td>
<td>Coolant, Stainless Steel</td>
</tr>
<tr>
<td>2 - 6</td>
<td>Core Zones</td>
<td>Coolant, Fuel, Zr, Control Rods</td>
</tr>
<tr>
<td>7</td>
<td>Lower Internals (includes inlet plenum, spacer pins, etc.)</td>
<td>Coolant, Stainless Steel</td>
</tr>
<tr>
<td>8 - 14</td>
<td>Homogenized Downcomer (includes core liner, water gaps, thermal shield, core barrel and downcomer)</td>
<td>Coolant, Stainless Steel</td>
</tr>
<tr>
<td>15</td>
<td>Reactor Vessel</td>
<td>Carbon Steel</td>
</tr>
<tr>
<td>16</td>
<td>Air Gap</td>
<td>Standard Air</td>
</tr>
<tr>
<td>17</td>
<td>Detector</td>
<td>Lead, Polyethylene, BF$_3$</td>
</tr>
<tr>
<td>18</td>
<td>Biological Shield</td>
<td>Concrete</td>
</tr>
</tbody>
</table>

The number density information for the basic materials is presented in Tables A-2 through A-4. Generally, the number densities were taken directly from the NSAC model description. If a material was not included in the NSAC model, e.g., polyethylene, the number density was created from first principles. Certain trace nuclides in some materials were omitted in the interest of expediency: e.g., F, Si and Mn. Their neglect has virtually no impact upon the neutronics of the material properties. Other trace nuclides, whose cross sections were unavailable on a timely basis, were approximated via a
Fig. A-1. Calculational RZ Model Geometry of TMI-2 Reactor out to the Biological Shield

Fig. A-2. Expanded Details of the Source Range Detector Area
simple nuclide substitution scheme. When a nuclide was to be replaced, an available nuclide with similar neutronic properties was chosen as its substitute. The relative proportions of thermal capture, scattering and the resonance integral value from BNL-325 were compared among the original nuclide and 3 arbitrary candidates for substitution: Cr, Fe and Ni. That isotope which most closely matched the proportions for the original nuclide was selected. The equivalent number density was then set by ratioing the thermal \((n,\gamma)\) cross section value of the two nuclides. Table A-2 illustrates the resulting equivalences which nominally preserve thermal capture reaction rates.

Table A-3 illustrates the implementation of the trace nuclide replacement scheme upon the reactor vessel carbon steel. As can be seen, changes are minor with respect to the total composition. Given that the replaced nuclides constitute a very small portion of the total material, it is deemed adequate to represent them in such an approximate fashion.

Soluble boron and both the burnable poison \((B_4C)\) and control material were modeled as an equivalent amount (reactivity-wise) of B-10. This
### TABLE A-4. Homogenized Number Densities: TMI-2 KZ Calculational Model

<table>
<thead>
<tr>
<th>Nuclide</th>
<th>1 Upper Internals</th>
<th>2 + 6 Core Zones</th>
<th>7 Lower Internals</th>
<th>8 - 14 Homogenized Downcomer</th>
<th>15 Reactor Vessel</th>
<th>16 Air</th>
<th>17a Detector Shield</th>
<th>17b Detector Polyethylene</th>
<th>17c Active Zone</th>
<th>18 Biological Shield</th>
</tr>
</thead>
<tbody>
<tr>
<td>H</td>
<td>((1-v)\times10^{-2})</td>
<td>((1-v)3.1296\times10^{-2})</td>
<td>((1-v)2.2333\times10^{-2})</td>
<td>((1-v)0.9978\times10^{-2})</td>
<td>((1-v)0.7930\times10^{-2})</td>
<td>((1-v)0.6039\times10^{-2})</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>U</td>
<td>((1-v)2.3328\times10^{-3})</td>
<td>((1-v)1.5648\times10^{-3})</td>
<td>((1-v)1.2752\times10^{-3})</td>
<td>((1-v)0.9558\times10^{-3})</td>
<td>((1-v)0.920\times10^{-3})</td>
<td>((1-v)0.920\times10^{-3})</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>235U</td>
<td>1.4974 \times10^{-3}</td>
<td>((1-v)2.1143\times10^{-3})</td>
<td>((1-v)1.9458\times10^{-3})</td>
<td>((1-v)1.0434\times10^{-3})</td>
<td>((1-v)1.0434\times10^{-3})</td>
<td>((1-v)1.0434\times10^{-3})</td>
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<td>238U</td>
<td>6.3519 \times10^{-3}</td>
<td>((1-v)0.905\times10^{-3})</td>
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<td>239Pu</td>
<td>1.0695 \times10^{-3}</td>
<td>((1-v)4.1537\times10^{-3})</td>
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<td>((1-v)4.1537\times10^{-3})</td>
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<tr>
<td>Zr</td>
<td>4.1537 \times10^{-3}</td>
<td>((1-v)9.2338\times10^{-3})</td>
<td>((1-v)3.1939\times10^{-3})</td>
<td>((1-v)3.6899\times10^{-3})</td>
<td>((1-v)3.6899\times10^{-3})</td>
<td>((1-v)3.6899\times10^{-3})</td>
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<tr>
<td>108 (^{108})</td>
<td>((1-v)4.6684\times10^{-3})</td>
<td>((1-v)9.2338\times10^{-3})</td>
<td>((1-v)1.939\times10^{-3})</td>
<td>((1-v)3.6899\times10^{-3})</td>
<td>((1-v)3.6899\times10^{-3})</td>
<td>((1-v)3.6899\times10^{-3})</td>
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<tr>
<td>Fe</td>
<td>((1-v)6.6201\times10^{-3})</td>
<td>((1-v)1.1440\times10^{-3})</td>
<td>((1-v)1.5517\times10^{-3})</td>
<td>((1-v)8.1905\times10^{-3})</td>
<td>((1-v)8.1905\times10^{-3})</td>
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<tr>
<td>Cr</td>
<td>((1-v)1.9826\times10^{-3})</td>
<td>((1-v)3.4229\times10^{-3})</td>
<td>((1-v)4.5278\times10^{-3})</td>
<td>((1-v)1.7246\times10^{-3})</td>
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<td>Ni</td>
<td>((1-v)1.4921\times10^{-3})</td>
<td>((1-v)2.5778\times10^{-3})</td>
<td>((1-v)3.4153\times10^{-3})</td>
<td>((1-v)7.0678\times10^{-3})</td>
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<td>((1-v)2.670\times10^{-3})</td>
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<tr>
<td>C</td>
<td>((1-v)8.670\times10^{-3})</td>
<td>((1-v)2.170\times10^{-3})</td>
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<td>Pb</td>
<td>((1-v)2.0885\times10^{-3})</td>
<td>((1-v)1.5783\times10^{-3})</td>
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<tr>
<td>Xe</td>
<td>((1-v)4.2171\times10^{-3})</td>
<td>((1-v)1.089\times10^{-3})</td>
<td>((1-v)1.089\times10^{-3})</td>
<td>((1-v)1.089\times10^{-3})</td>
<td>((1-v)1.089\times10^{-3})</td>
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<tr>
<td>Sm</td>
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<td>((1-v)1.089\times10^{-3})</td>
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<td>((1-v)1.089\times10^{-3})</td>
<td>((1-v)1.089\times10^{-3})</td>
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</table>

* a Read as \(4.6684 \times 10^{-3}\), with \(v\) representing the coolant void fraction.

b The two components represent the coolant water and the UO2 contributions, respectively.
resulted in the control rod material being replaced with ~1000 ppm, the burnable poison represented as ~440 ppm, and the soluble boron level set at ~1160 ppm for a nonvoided coolant. The total equivalent poison is thus on the order of 2600 ppm. As voiding was modeled, the void fraction acted only upon that boron which represented the contribution from soluble boron. Table A-4 lists the homogenized material number densities, as utilized in the calculational model. They correspond directly with the region numbering in Table A-1 and, of course, already reflect the appropriate volume fractions.